

The Base Functions of the RELVIEW System, Version 7.0*

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The base functions of RELVIEW can be divided into several parts:

1. Base functions for calculating constant relations and domains:

Syntax	Meaning
$L(R)$	Universal relation with the same dimension as R
$0(R)$	Empty relation with the same dimension as R
$I(R)$	Identity relation with the same dimension as R
$Ln1(R)$	Universal column vector with the same row number as R
$On1(R)$	Empty column vector with the same row number as R
$L1n(R)$	Universal row vector with the same column number as R
$O1n(R)$	Empty row vector with the same column number as R
$dom(R)$	Domain $R * Ln1(R^{\wedge})$ of relation R as column vector

2. Base functions for calculating Boolean operations:

Syntax	Meaning
$\neg R$	Negation (complement) of relation R
$R \mid S$	Union (join) of R and S
$R \& S$	Intersection (meet) of R and S

3. Base functions for calculating relationalgebraic operations:

Syntax	Meaning
R^{\wedge}	Transposition of relation R
$R * S$	Composition (product) of R and S

4. Base functions for calculating residuals and symmetric quotients:

Syntax	Meaning
S / R	Left residual of R and S
$R \backslash S$	Right residual of R and S
$syq(R, S)$	Symmetric quotient of R and S

*WWW: <http://www.informatik.uni-kiel.de/~progsys/relview.shtml>

5. Base functions for calculating closures:

Syntax	Meaning
trans (R)	Transitive closure of R
refl (R)	Reflexive closure of R
symm (R)	Symmetric closure of R

6. Various base functions concerning vectors and points without choice operations:

Syntax	Meaning
inj (v)	Injection induced by the non-empty vector v
init (v)	Initial point with the same dimension as the vector v
succ (v)	Homogeneous successor relation with a dimension given by the number of rows of the vector v
next (p)	Successor of the point p with the same dimension as p

7. Base operations for choices:

Syntax	Meaning
point (v)	A point included in the non-empty column vector v
atom (R)	An atom (a relation consisting of one pair) included in the non-empty relation R

8. Base operations which generate random relations. In the following, XY stands for two digits between 00 and 99 and denotes the probability that a pair is contained in the result:

Syntax	Meaning
randomXY (R)	Generation of a random relation with the same dimension as R
randomcfXY (R)	Generation of a cyclefree random relation with the same dimension as the homogeneous relation R
randomperm (v)	Generation of a random permutation, where the dimension is given by the number of rows of the vector v

9. Base functions for certain tests on relations. The result is *true* (represented by the universal relation on a singleton set) or *false* (represented by the empty relation on a singleton set):

Syntax	Meaning
empty (R)	Test, whether R is empty
unival (R)	Test, whether R is univalent
eq (R,S)	Test, whether R and S are equal
incl (R,S)	Test, whether R is included in S
cardeq (R,S)	Test, whether the cardinalities of R and S are equal
cardlt (R,S)	Test, whether the cardinality of R is less than that of S
cardgt (R,S)	Test, whether the cardinality of R is greater than that of S

10. Base functions concerning operations on powersets:

Syntax	Meaning
<code>epsi(v)</code>	Membership relation, where the cardinality of the base set is given by the row number of the vector \mathbf{v}
<code>cardrel(v)</code>	Size comparison relation on a powerset, where the cardinality of the base set is given by the row number of the vector \mathbf{v}
<code>cardfilter(v,w)</code>	If \mathbf{v} is a vector with a powerset 2^X as argument set and \mathbf{w} is a vector with $n \leq X + 1$ columns, then the operation selects from \mathbf{v} all sets s fulfilling $ s < n$

11. Base functions concerning relational product and sum domains. Most of these base functions take a domain definition as argument, the result however is always a relation:

Syntax	Meaning
<code>1-st(DD)</code>	1st component (DD domain)
<code>2-nd(DD)</code>	2nd component (DD domain)
<code>p-1(PP)</code>	Projection onto the 1st component (PP product domain)
<code>p-2(PP)</code>	Projection onto the 2nd component (PP product domain)
<code>p-ord(PP)</code>	Product order (PP product domain)
<code>[R,S]</code>	Tupling of relations
<code>i-1(SS)</code>	Injection into 1st component (SS sum domain)
<code>i-2(SS)</code>	Injection into 2nd component (SS sum domain)
<code>s-ord(SS)</code>	Sum order (SS sum domain)
<code>R + S</code>	Sum of relations

12. Base functions concerning function domains:

Syntax	Meaning
<code>part-f(R,S)</code>	Columnwise representation of partial functions
<code>tot-f(R,S)</code>	Columnwise representation of total functions